

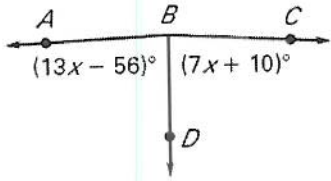
# Tour de Geometry

## Stage 1 Semester 1

★ use appropriate units in your answers!  
 (and symbols)

Team Name: Key

1)  $\overline{BD}$  bisects  $\angle ABC$ . Find the value of  $x$ .



$$13x - 56 = 7x + 10$$

$$6x = 66$$

$$x = 11$$

$$\underline{x = 11}$$

2) The measure of  $XZ$  is 27. Find the value of  $x$ .



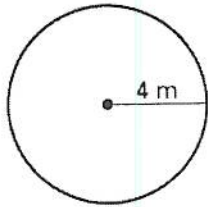
$$5x + 2 = 27$$

$$5x = 25$$

$$\underline{x = 5}$$



3) Find the area of the circle. use  $\pi$  button



$$A = \pi r^2$$

$$\frac{50.24 \text{ m}^2}{50.27 \text{ m}^2}$$

4) The expression  $-2x + 41$  and  $7x - 40$  represent the length of two sides of a regular pentagon. Find the length of each side of the pentagon.

$$-2x + 41 = 7x - 40$$

$$41 = 9x - 40$$

$$81 = 9x$$

$$x = 9$$

$$63 - 40$$

$$\underline{23}$$

all sides  $\cong$

5)  $\angle 1$  and  $\angle 2$  are supplementary angles. If the measure of  $\angle 2 = 115^\circ$ , find the  $m\angle 1$ .

$$180 - 115$$

$$\underline{65^\circ}$$

Use the diagram for questions 6 and 7.

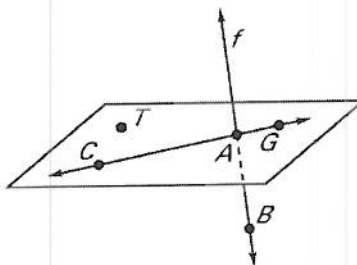
6) Name **two** intersecting lines.

$\overleftrightarrow{CG}$   $\overleftrightarrow{AB}$

$\overleftrightarrow{AG}$  line  $f$

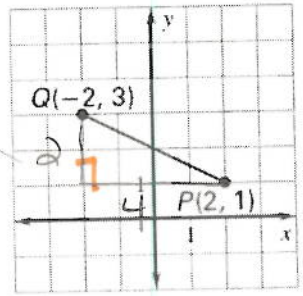
BAGT  
CBAG

so many



7) Name **four** non-coplanar points.

8) Find the length of the segment. *answer in simplified form* 2√5



$$4 + 16 = c^2$$

$$20 = c^2$$

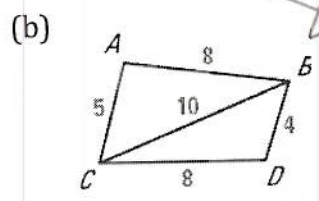
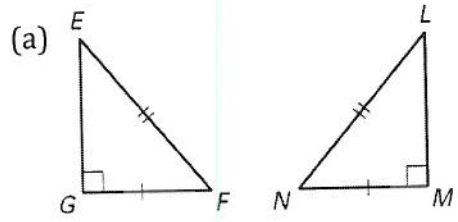
$$2\sqrt{5}$$

$$\sqrt{(16) + (4)}$$

$$\sqrt{(2+2)^2 + (1-3)^2}$$

$$(-2)^2 = -4$$

9) Can you show the triangles are congruent? If so, which theorem or postulate would you use?

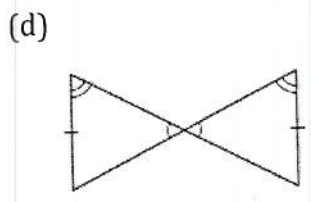
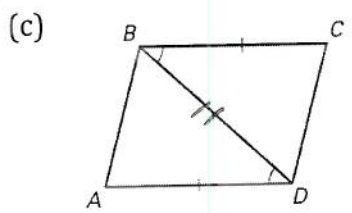


a) yes HL

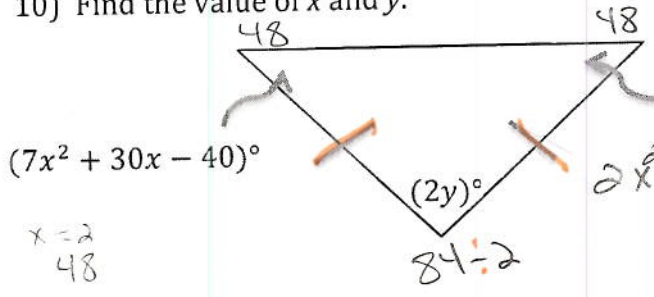
b) NO

c) yes SAS

d) yes AAS



10) Find the value of x and y.



x = 2

y = 42

$$2x^2 - 15x + 70 = 7x^2 + 30x - 40$$

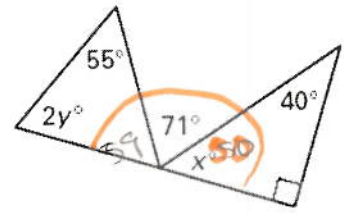
$$0 = 5x^2 + 45x - 110$$

$$0 = 5(x^2 + 9x - 22)$$

$$0 = 5(x+11)(x-2)$$

x = -11, 2

11) Find the value of x and y.



x = 50°

y = 33

12) Solve the proportion.

$$\frac{2z}{27} = \frac{3z+9}{81}$$

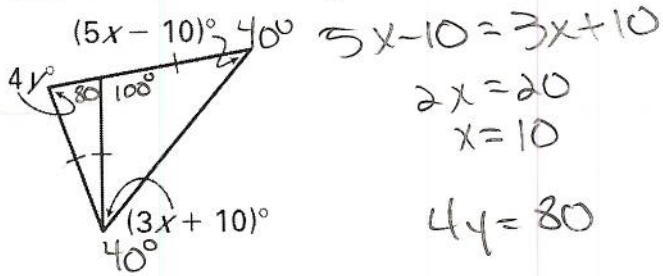
$$2z(81) = 27(3z+9)$$

$$162z = 81z + 243$$

$$81z = 243$$

z = 3

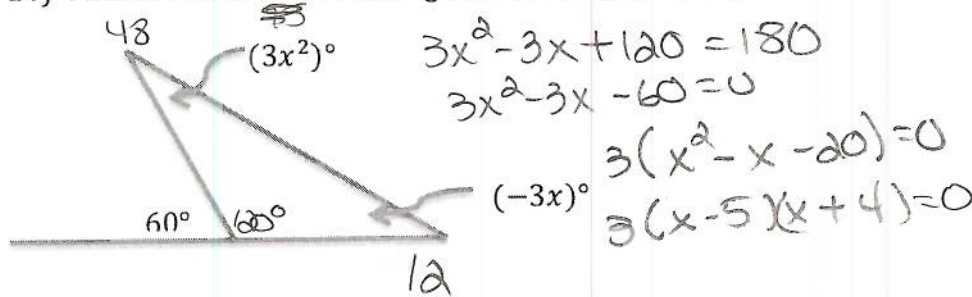
13) Find the values of x and y.



$x = 10$

$y = 20$

14) Find the value of x in the figure to the right. After, find the measure of each interior angle.



$x = -4$

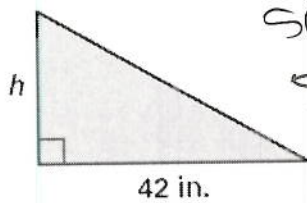
$120^\circ, 48^\circ, 12^\circ$

$(1, \frac{5}{2})$

15) Find the midpoint between points A and B.

$A(10, 2)$  and  $B(-8, 3)$   $(\frac{2}{2}, \frac{5}{2})$

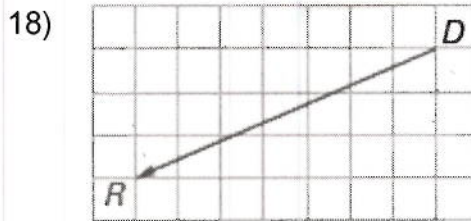
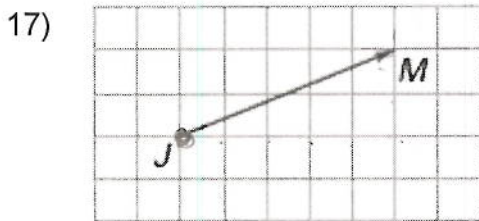
16) The area of the triangle is 504 square inches. Find the height.



$504 = \frac{1}{2} \cdot 42 \cdot h$   
 $504 = 21 \cdot h$

$h = 24 \text{ in.}$

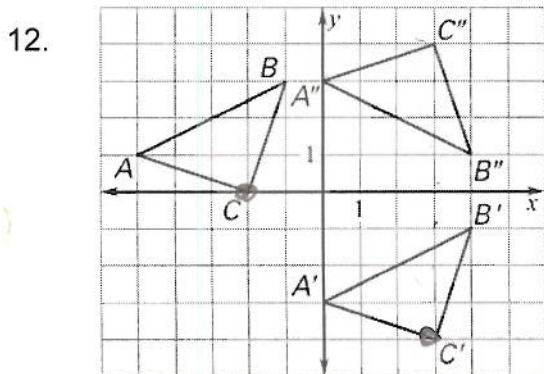
Name the vector and write it in its component form.



$\vec{JM} \langle 5, 2 \rangle$

$\vec{DR} \langle -7, -3 \rangle$

Describe the rule for each transformation.



$ABC \rightarrow A'B'C'$   
 $A'B'C' \rightarrow A''B''C''$  reflection over x-axis  
 $12. (x+5, y-4)$

# Tour de Geometry

Stage 2 Semester 1

Team Name: Key

Multiply the matrices, if possible.

1) 
$$\begin{bmatrix} 4 & -3 \end{bmatrix}_{1 \times 2} \begin{bmatrix} -6 \\ 2 \end{bmatrix}_{2 \times 1}$$
  

$$\begin{bmatrix} -30 \end{bmatrix}$$

2) 
$$\begin{bmatrix} -2 & 3 \\ 5 & -4 \end{bmatrix} \begin{bmatrix} -1 & 4 \\ 7 & 5 \end{bmatrix}$$

1. 
$$\begin{bmatrix} -30 \end{bmatrix}$$

2. 
$$\begin{bmatrix} 23 & 7 \\ -33 & 0 \end{bmatrix}$$

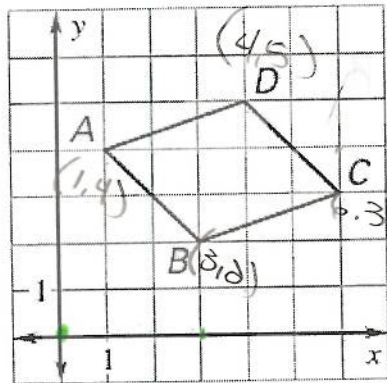
3. 
$$\begin{bmatrix} -9 & -3 \\ 7 & 2 \\ 2 & 1 \end{bmatrix}$$

3) 
$$\begin{bmatrix} -3 & 3 \\ 3 & -2 \\ 0 & -1 \end{bmatrix}_{3 \times 2} \begin{bmatrix} 1 & 0 \\ -2 & -1 \end{bmatrix}_{2 \times 2}$$

Find the coordinates of the vertices of the figures after a dilation by the given scale factor.

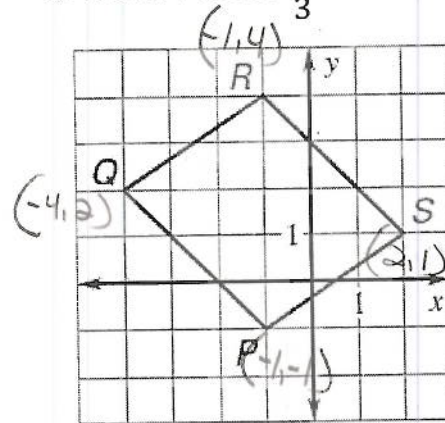
*★ Fraction answers*

4. Scale Factor: 2



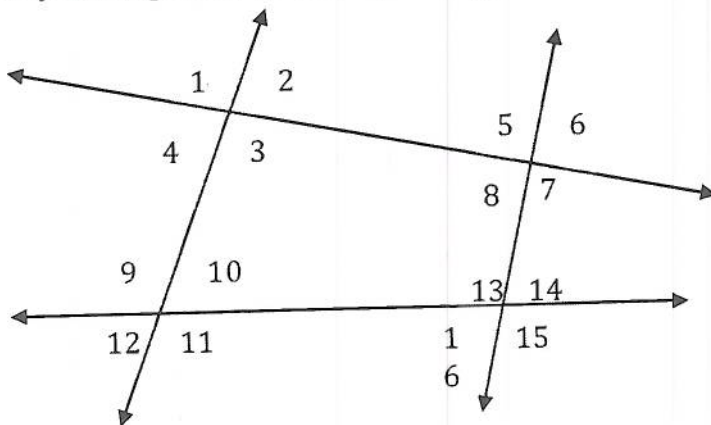
- A (2, 4)
- B (8, 0)
- C (12, 6)
- D (4, 5)

5. Scale Factor:  $\frac{2}{3}$



- P  $(-\frac{2}{3}, -\frac{2}{3})$
- Q  $(-\frac{8}{3}, \frac{4}{3})$
- R  $(-\frac{2}{3}, \frac{8}{3})$
- S  $(\frac{4}{3}, \frac{2}{3})$

6) Classify the angle pair as *corresponding*, *alternate interior*, *alternate exterior*, or *consecutive interior*.



$\angle 1$  and  $\angle 11$  alt.

$\angle 2$  and  $\angle 5$  cons. int.

$\angle 15$  and  $\angle 11$  corr.  
*(not  $\cong$  b/c lines not  $\parallel$ )*

$\angle 8$  and  $\angle 14$  alt. int.

(S2 P2)

7) The measure of one angle is three times the measure of its complement. Find the measure of each angle.

$x = 1^{st} \angle$   
 $y = 2^{nd} \angle$   
 (complement)

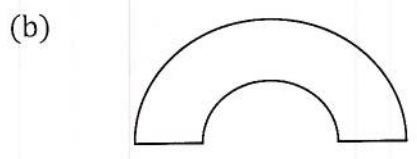
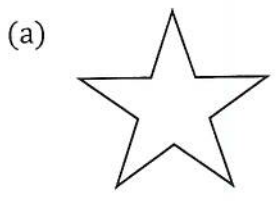
$3y = x$   
 $x + y = 90$

substitute  
 $3y + y = 90$   
 $4y = 90$

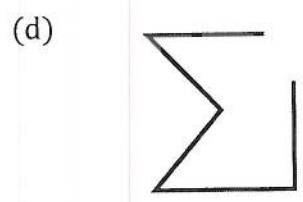
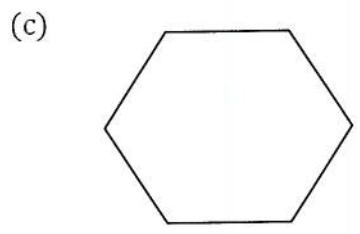
$y = 22.5^\circ$   
 $x = 67.5^\circ$

8) Decide whether the figure is a polygon.

8) Also, how many lines of symmetry? rotational symmetry?



(a) yes, 5 l.o.s.  
 $72^\circ, 144^\circ$  rot. sym.

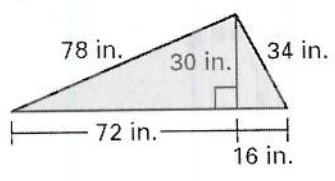


(b) no, 1 l.o.s.,  
 no rotational

(c) yes, 6 l.o.s.  
 $60^\circ, 120^\circ, 180^\circ$  rot.

(d) no

9) Find the perimeter and the area of the triangle.

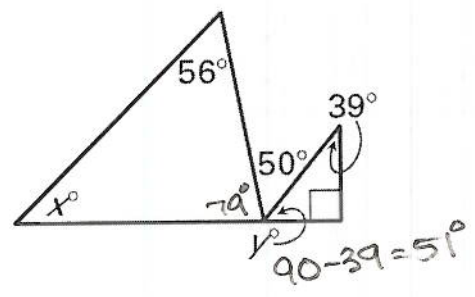


don't need

P = 200 in.

A = 1320 in.<sup>2</sup>

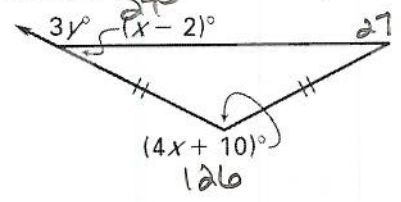
10) Find the values of x and y.



x = 45

y = 51

11) Find the values of x and y.



$2(x-2) + 4x + 10 = 180$   
 $6x + 6 = 180$   
 $6x = 174$   
 $x = 29$

x = 29

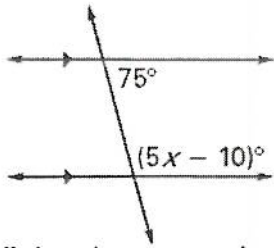
y = 51

$180 - 27 = 34$  OR  
 $153 = 34$

Ext.  $\angle$  theorem  
 $126 + 27 = 34$   
 $153 = 34$

12) Find the value of  $x$ .

[52 p 3]



$$75 + 5x - 10 = 180$$

$$x = 23$$

13) Solve the proportion

$$\frac{2x}{x+15} = \frac{-1}{x-6}$$

$$2x(x-6) = -x-15$$

$$2x^2 - 12x = -x - 15$$

$$x^2 - 11x + 15 = 0$$

$$(x-3)(2x-5) = 0$$

$$x-3=0 \quad 2x-5=0$$

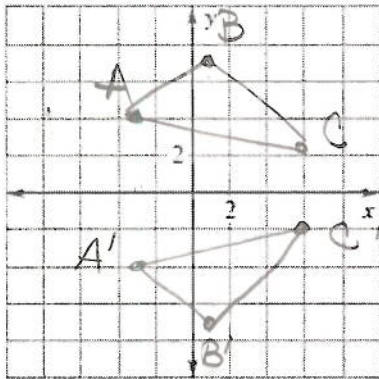
$$x=3$$

$$x=5/2$$



Perform the given transformation.

14. Reflect  $\begin{bmatrix} A & B & C \\ -3 & 1 & 6 \\ 4 & 7 & 2 \end{bmatrix}$  in the  $x$ -axis.



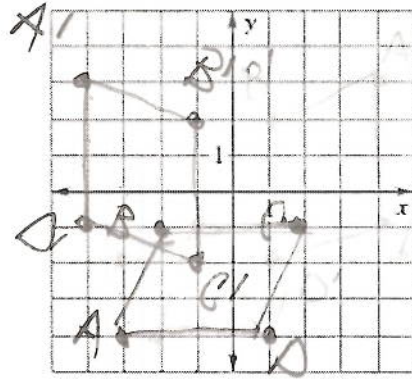
$y$  coord opposite

$$A'(-3, -4)$$

$$B'(1, -7)$$

$$C'(6, -2)$$

15.  $\begin{bmatrix} A & B & C & D \\ -3 & -2 & 2 & 1 \\ -4 & -1 & -1 & -4 \end{bmatrix}; 270^\circ$



switch  $x, y$   
both opposite

$$A'(-4, 3)$$

$$B'(1, 2)$$

$$C'(-1, 2)$$

$$D'(-4, -1)$$

16.  $\begin{bmatrix} A & B & C \\ 3 & 1 & 5 \\ 1 & 5 & 3 \end{bmatrix}$

Translation:  $(x, y) \rightarrow (x - 6, y + 1)$

Rotation:  $90^\circ$  about the origin

$$A'(-3, 2)$$

$$A''(-2, 3)$$

$$B'(-5, 6)$$

$$B''(-6, -5)$$

$$C'(-1, 4)$$

$$C''(-4, -1)$$

$y$ -axis  $(-x, y)$

$x$ -axis  $(x, -y)$

$y=x$   $(y, x)$

$90^\circ$   $(-y, x)$

$180$   $(-x, -y)$

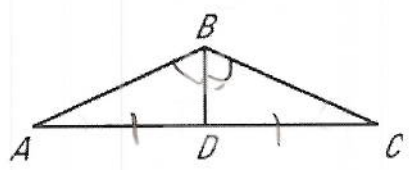
$270^\circ$   $(y, -x)$

Use the diagram and the given information to list all possible names for segment  $BD$ .

17)  $\overline{AD} \cong \overline{CD}$

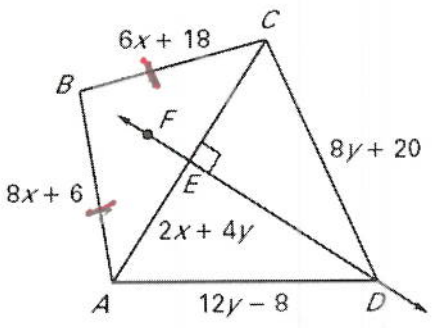
18)  $\overline{BD} \perp \overline{AC}$  and  $\overline{AD} \cong \overline{CD}$

19)  $\angle ABD \cong \angle CBD$



- BD median
- $\perp$  bisector
- altitude
- angle bisector
- median

20)  $DE$  is the perpendicular bisector of  $AC$ . Find the indicated measures.



$AD = \underline{76}$

$AB = \underline{54}$

$AE = \underline{40}$

$AC = \underline{80}$

$$12y - 8 = 8y + 20$$

$$12y = 8y + 28$$

$$4y = 28$$

$$y = 7$$

$$AD = 12(7) - 8$$

$$6x + 18 = 8x + 6$$

$$12 = 2x$$

$$x = 6$$

$$AB = 8(6) + 6$$

$$AE = 2(6) + 4(7)$$

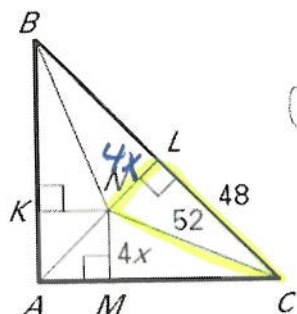
# Tour de Geometry

## Stage 3 Semester 1

Team Name: Key

1) Find the value of  $x$  that makes  $N$  the **incenter**.

1)  $x = 5$



$$(4x)^2 + 48^2 = 52^2$$

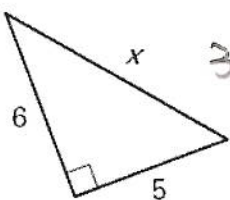
$$16x^2 + 2304 = 2704$$

$$16x^2 = 400$$

$$x^2 = 25$$

2) Find the missing length in simplest radical form.

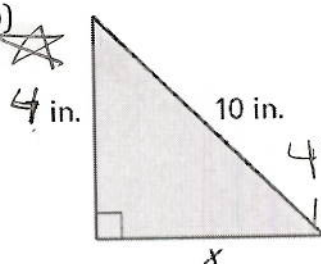
(a)



$$36 + 25 = x^2$$

$$61 = x^2$$

(b)



$$4^2 + x^2 = 10^2$$

$$16 + x^2 = 100$$

$$x^2 = 84$$

a)  $x = \pm\sqrt{61}$

b)  $x = \pm 2\sqrt{21}$

Add or subtract the matrices.

3.

$$\begin{bmatrix} 5 & -2 \\ 2 & 4 \\ -7 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 3 \\ 6 & -4 \\ 6 & -1 \end{bmatrix}$$

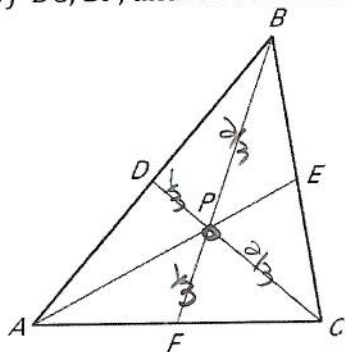
4.

$$[-0.3 \quad 1.8] - [0.6 \quad 2.7]$$

$$\begin{bmatrix} 6 & 1 \\ 8 & 0 \\ -1 & 1 \end{bmatrix}$$

$$[-.9 \quad -.9]$$

5)  $DC$ ,  $BF$ , and  $AE$  are medians. (a) What is point  $P$  called? (b) If  $BF = 15$ , find  $BP$  and  $PF$ .



a) Centroid

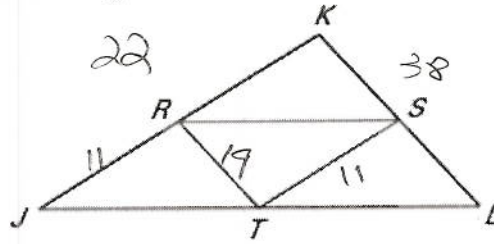
$BP =$  10

$PF =$  5



In the diagram below,  $RS$ ,  $RT$ , and  $ST$  are midsegments.

6) If  $KL$  is 38, find  $RT$



RT = 19

7) If  $ST$  is 11, find  $RJ$

RJ = 11

8) The measure of the angles of a triangle are in the ratio of 2:4:5. Find the measures of each angle.

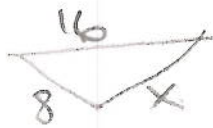
13

Angle 1: \_\_\_\_\_

Angle 2: \_\_\_\_\_

Angle 3: \_\_\_\_\_

9) A triangle has one side length of 8 and another length 16, write an inequality describing the possible lengths of the third side.



$8 + 16 > x$

$8 + x > 16$

~~$16 + x > 8$~~   
 $x > -8$

$x < 24$

$x > 8$

$8 < x < 24$

per look @ both exp.  
ch. 5  
Mr. Newman 5.1-5.5 notes  
end of chapter