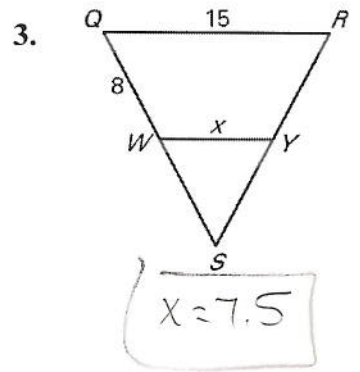
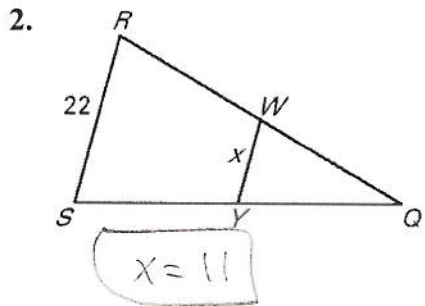
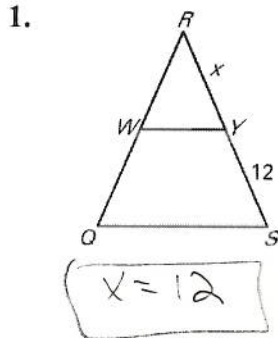
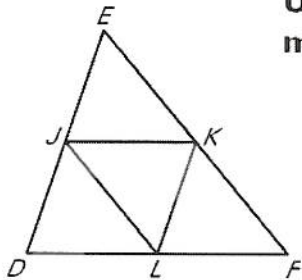


## 5.1-5.3 Quiz Review – Geometry 9

***WY* is the midsegment of  $\triangle QRS$ . Find the value of  $x$ .**



**Use  $\triangle DEF$ , where  $J$ ,  $K$ , and  $L$  are midpoints of the sides.**



4. If  $DE = 8x + 12$  and  $KL = 10x - 9$ , what is  $DE$ ?

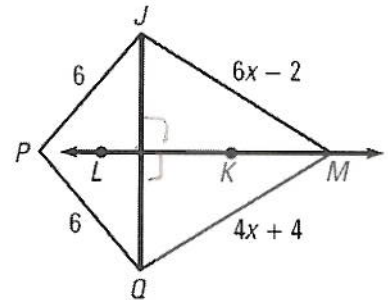
$$\begin{aligned} 2(10x - 9) &= 8x + 12 \\ 20x - 18 &= 8x + 12 \\ 12x &= 30 \\ x &= 2.5 \end{aligned}$$

$$\begin{aligned} DE &= 8(2.5) + 12 \\ \boxed{DE} &= \boxed{32} \end{aligned}$$

5. In the diagram,  $\overline{LM}$  is the perpendicular bisector of  $\overline{JQ}$ , and point  $K$  lies along  $\overline{LM}$ .

a. Find the value of  $x$ .

$$\begin{aligned} 6x - 2 &= 4x + 4 \\ 6x &= 4x + 6 \\ 2x &= 6 \\ \boxed{x} &= \boxed{3} \end{aligned}$$



b. Find  $JM$ .

$$\begin{aligned} 6(3) - 2 &= 16 \\ \boxed{JM} &= \boxed{16} \end{aligned}$$

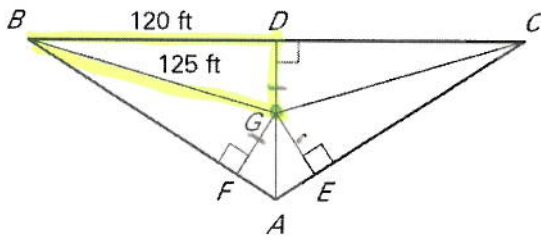
c. Identify two points that are the same distance from point  $K$ .

$\boxed{J \ \& \ Q}$

d. Is  $P$  guaranteed to be on line  $\overline{LM}$ , or not? State why.

yes, because of the  $\perp$  bisector converse.

6. **Monument** You are building a monument in a triangular park. You want the monument to be the same distance from each edge of the park. Use the figure with incenter  $G$  to determine how far from point  $D$  you should build the monument.



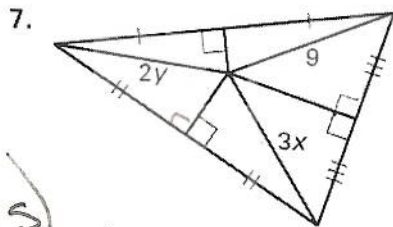
$$120^2 + b^2 = 125^2$$

$$b^2 = 1225$$

$$b = 35$$

$$DG = 35 \text{ ft}$$

Find the value of  $x$ . Then find the value of  $y$ .



(by SAS)  
(CPCTC)

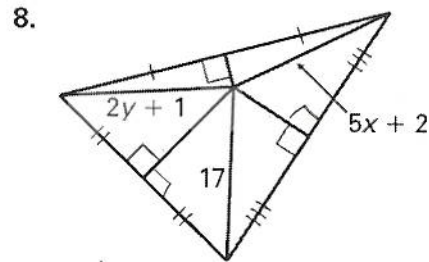
$$3x = 9$$

$$x = 3$$

$$2y = 9 \text{ (also by SAS)}$$

$$y = 4.5$$

(CPCTC)



$$17 = 5x + 2$$

$$15 = 5x$$

$$x = 3$$

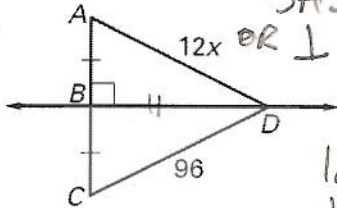
$$2y + 1 = 17$$

$$2y = 16$$

$$y = 8$$

Find the value of  $x$ . Identify the theorem used to find the answer.

9.

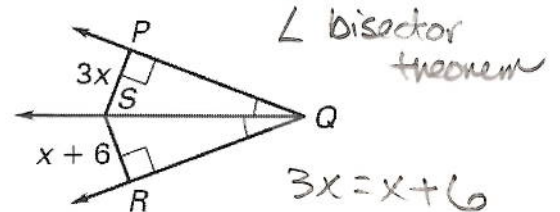


SAS-CPCTC  
OR  $\perp$  bisector theorem

$$12x = 96$$

$$x = 8$$

10.



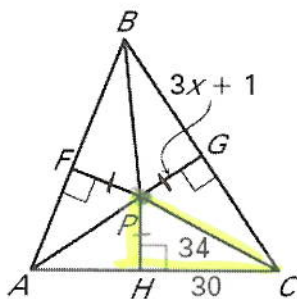
$\angle$  bisector theorem

$$3x = x + 6$$

$$2x = 6$$

$$x = 3$$

Find the value of  $x$  that makes  $P$  the incenter of the triangle.



$$\Delta PHC$$

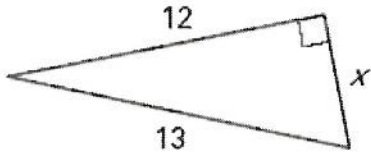
$$x^2 + 30^2 = 34^2$$

$$x^2 = 256$$

$$x = 16$$

Find the missing measurements. Leave your answer in simplest radical form.

6)

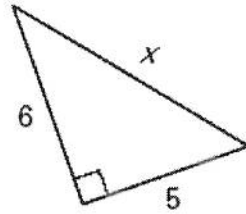


$$x^2 + 12^2 = 13^2$$

$$x^2 = 25$$

$$x = 5$$

7)

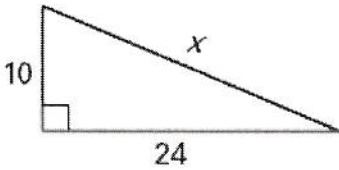


$$5^2 + 6^2 = x^2$$

$$61 = x^2$$

$$x = \sqrt{61}$$

8)

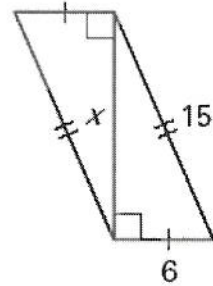


$$10^2 + 24^2 = x^2$$

$$676 = x^2$$

$$x = 26$$

9)



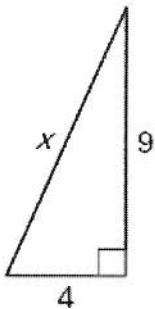
$$x^2 + 6^2 = 15^2$$

$$\sqrt{x^2} = \sqrt{189}$$

$$x = \sqrt{9} \cdot \sqrt{21}$$

$$x = 3\sqrt{21}$$

10)

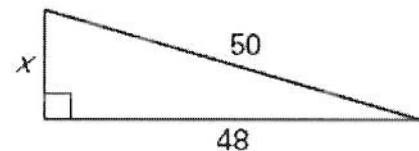


$$4^2 + 9^2 = x^2$$

$$x^2 = 97$$

$$x = \sqrt{97}$$

11)



$$48^2 + x^2 = 50^2$$

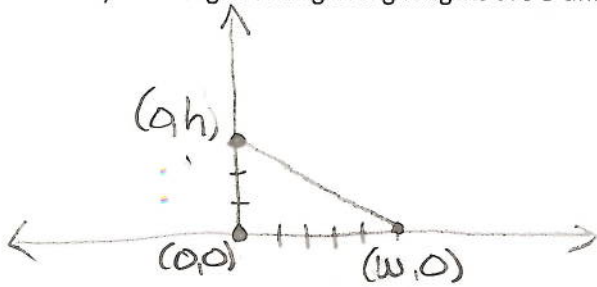
$$x^2 = 196$$

$$x = 14$$

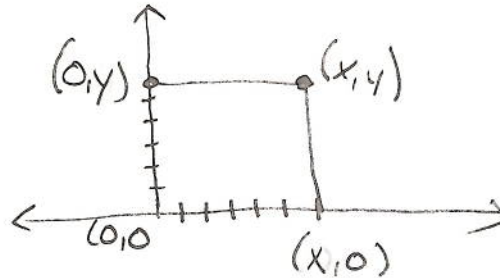
Using Variable Coordinates

Place the figure in a coordinate plane in a convenient way and assign coordinates to each vertex.

1) Right Triangle: leg lengths are 5 units and 3 units.

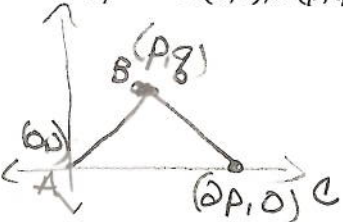


2) Square: side lengths are 6 units



Sketch  $\triangle ABC$ . After, find the length, slope, and midpoint of each side.

3)  $A(0,0), B(p,q), C(2p,0)$

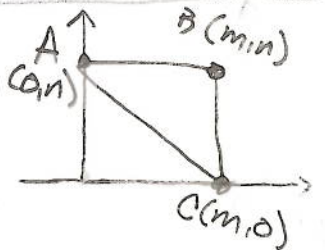


Length  $AC = 2p$   
 $AB = \sqrt{p^2 + q^2}$   
 $BC = \sqrt{(2p-p)^2 + (-q)^2}$   
 $= \sqrt{p^2 + q^2}$

Slope  $AC: 0$   
 $AB: \frac{q}{p}$   
 $BC: \frac{q-0}{2p-p} = \frac{q}{p}$

midpt  $AC: (p, 0)$   
 $AB: (\frac{p}{2}, \frac{q}{2})$   
 $BC: (\frac{3p}{2}, \frac{q}{2})$

4)  $A(0,n), B(m,n), C(m,0)$

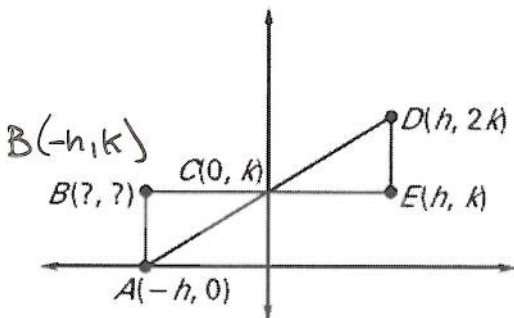


Length  $AB = m$   
 $BC = n$   
 $AC = \sqrt{m^2 + n^2}$

slope  $AB: 0$   
 $BC: \text{undefined}$   
 $AC: -\frac{n}{m}$

midpt  
 $AB: (\frac{m}{2}, n)$   
 $BC: (m, \frac{n}{2})$   
 $AC: (\frac{m}{2}, \frac{n}{2})$

5) First, find the coordinates of point B. Then, show  $\triangle ABC \cong \triangle DEC$ . Hint: Show SSS congruence is true. or SAS



Distance

$BC = \sqrt{(k-k)^2 + (0-h)^2}$      $EC = \sqrt{(h-0)^2 + (k-k)^2}$   
 $BC = h$      $EC = h$

so  $\overline{BC} \cong \overline{EC}$

$AC = \sqrt{(-h-0)^2 + (0-k)^2}$      $DC = \sqrt{(h-0)^2 + (2k-k)^2}$   
 $= \sqrt{h^2 + k^2}$      $DC = \sqrt{h^2 + k^2}$

$AC = \sqrt{h^2 + k^2}$

$\overline{AC} \cong \overline{DC}$

$\angle BCA \cong \angle DCE$  by vertical  $\angle$ 's  
 so  $\triangle ABC \cong \triangle DEC$  by SAS